Neighbor Discovery and Rendezvous Maintenance with Extended Quorum Systems for Mobile Applications

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Abstract—In many mobile sensing applications devices need to discover new neighbors and maintain the rendezvous with known neighbors continuously. Due to the limited energy supply, these devices have to duty cycle their radios to conserve the energy and bandwidth, making neighbor discovery and rendezvous maintenance even more challenging. To date, the main mechanism for device discovery and rendezvous maintenance in existing solutions is pairwise, direct one-hop communication. We argue that such pairwise direct communication is sufficient but not necessary: there exist unnecessary active slots that can be eliminated, without affecting discovery and rendezvous. In this work, we propose a novel concept of extended quorum system, which leverages indirect discovery to further conserve energy. Specifically, we use quorum graph to capture all possible information flow paths where knowledge about known-neighbors can propagate among devices. By eliminating redundant paths, we can reduce the number of active slots significantly. Since a quorum graph can characterize arbitrary active schedules of mobile devices, our work can be broadly used to improve many existing quorum-based discovery and rendezvous solutions. We comprehensively evaluate EQS in three different scales of networks, and the results show that EQS reduces as much as 55% energy consumption with a maximal 5% increase in latency for existing solutions. To test the real-world values of EQS, we further propose a taxicab dispatching application called EQS-dismiss to navigate taxicab drivers to the area with less competition based on the discovery results of nearby taxicabs.

Index Terms—Mobile Network, Neighbor Discovery, Quorum System.

1 INTRODUCTION

There has been a consistent rise of mobile sensing applications where devices equipped with various sensors interact with each other upon encounters [1] [2] [3] [4] [5] [6] [7]. These applications rely on neighbor discovery and rendezvous maintenance, where new neighbors should be detected timely and contacts with existing neighbors are maintained continuously. Due to the limited battery capacity and bandwidth, these devices usually adopt duty cycling mechanisms [8] that switch their radios between active and inactive slots to conserve energy. Such an energy constrained environment makes it challenging to discover a device’s previous unknown neighbors and maintain rendezvous with already discovered ones.

In the past, several neighbor discovery and rendezvous protocols for wireless sensor networks [9] [10] [11] [12] [13] [14] have been proposed. But they typically have two key drawbacks. First, they all use a pairwise discovery mechanism via direct one-hop communication. We argue that such a direct discovery is not always necessary. Devices can leverage the knowledge of each other, such that neighbors unknown to some devices can be discovered through other devices. Second, most of them [12] [13] [14] treats rendezvous maintenance as a rediscovery problem, even though a large number of neighbors have already been discovered. Both of these drawbacks lead to unnecessary active slots that can be eliminated to further conserve energy.

Based on these observations, we develop an extended quorum system, which relies on a legacy mathematical concept called quorum system [11] to achieve efficient neighbor discovery and rendezvous maintenance. The extended quorum system propagates known neighborhood information indirectly by bridging multiple pairwise communication, thus avoiding the need for full-mesh pairwise discovery, i.e., avoid the direct one-hop communication. Further, the extended quorum system utilizes the propagation of neighborhood information for the rendezvous maintenance to avoid the rediscovery mechanism. We characterize such information propagation paths of known neighbors using a proposed concept called quorum graph, and propose a reduction algorithm that eliminates redundant paths to reduce the number of active slots. This significantly improves the energy efficiency of the discovery process.

Specifically, we make the following contributions:

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To the best of our knowledge, we present the first neighbor discovery protocol that utilizes the known neighborhood information for both the discovery of new neighbors and the rendezvous maintenance of old neighbors. In particular, we propose a novel generic concept called quorum graph and investigate its property called reachability, which is equivalent to neighborhood information flow among mobile devices. Based on the reachability of a quorum graph, we propose the legacy quorum system and extended quorum system, which is a quorum graph satisfying indirect reachability among all devices, such that fewer active slots are required in order to reduce the energy used.

Based on the quorum graph, we formalize the quorum reachability minimization problem to reduce the energy waste due to the redundancy of reachability in a quorum graph. We prove its NP-hardness by reducing the set covering problem to one of its simplified version.

To address the quorum reachability minimization problem in practice, we design a heuristic algorithm EQS that reduces redundant pairwise reachability between discovered and undiscovered neighbors. It supports the device discovery and rendezvous maintenance with a significantly reduced number of active slots (i.e., less energy).

We comprehensively evaluate EQS in three scales of networks: (i) a small-scale testbed experiment with 11 TelosB devices, (ii) a middle-scale simulation with 100 mobile devices, and (iii) a large-scale evaluation based on the GPS data from 14,000 vehicles. The results show that EQS can reduce as much as 55% energy consumption with a maximal 5% increase on latency for existing protocols.

To prove the real-world value of EQS, we propose a taxicab dispatching application called EQS-dispatch to show how EQS can be employed by taxicab drivers to select a direction with fewer competing taxis based on the neighboring taxicab discovery. We further evaluate EQS-dispatch based on a 280 GB dataset consisting of 6 months of GPS traces of more than 14,000 taxis in the most crowded city in China, Shenzhen, with 17,150 people per KM². Our application shows that a taxicab driver increases the possibility of picking up a passenger by going to the direction with fewer competing taxicabs based on the neighbor discovery of EQS.

The rest of the paper is organized as follows. Sections 2 and 2 present our motivations and design goal. Section 3 describes theoretical background, followed by our main design EQS in Section 4. Sections 5, 6 and 7 evaluate EQS in three networks with different scales. Section 8 proposes our EQS based application. Section 9 discusses related work. Finally, Section 10 concludes the paper.

2 Motivations

Although the existing neighbor discovery protocols guarantee the bounded discovery latency [12] [13] [14], they result in unnecessary active slots (thus a waste of energy) because their discovery schemes are built on direct interactions for pairwise communication. To address such an energy waste, we aim to explore indirect interactions in discovery protocols in terms of energy conservation. In what follows, we first use discuss the indirect interactions, and then discuss the potential of using these indirect interactions to conserve the energy. Finally, we present the motivation for our design.

2.1 Indirect Interaction

For the traditional discovery and rendezvous protocols, the design goal is to ensure that every device can find other devices in the asynchronous networks with direct interactions by themselves, e.g., peer-to-peer communication. Our work is mainly motivated by the observation that these protocols based on direct interactions suffer from unnecessary active slots, and they are especially inefficient when some neighbors have already been discovered. On the other hand, in mobile applications, it is desirable for mobile devices to utilize as few active slots as possible to conserve the energy. To this end, we notice that in many scenarios, neighboring devices share common neighbors, which opens the possibility of indirect interaction for the discovery and rendezvous with fewer active slots. Therefore, we aim to explore how to leverage indirect interactions for better energy efficiency. In particular, the existing protocols typically overlook the fact that neighborhood information may be indirectly propagated in the networks during the interactions of devices, e.g., rendezvous among discovered devices. Such an indirect neighborhood information propagation may greatly assist the discovery and rendezvous process, if it is leveraged with existing discovery and rendezvous protocols.

Conceptually, the indirection interactions can be achieved by letting devices broadcast their two-hop neighbor tables in active slots during the neighbor discovery. As a result, for the discovery of new neighbors, a device $S$ can indirectly discover its new neighbors via the direct rendezvous with discovered neighbors; for the rendezvous with already discovered neighbors (i.e., obtaining the latest neighbor tables from them) a device $S$ can indirectly rendezvous with a device $B$ by the direct rendezvous with an intermediate device $A$, given $A$ and $B$ have already rendezvoused, and this indirect rendezvous between $S$ to $B$ is achieved by the fact that $A$ will pass the neighbor table of $B$ to $S$. Taking this indirect discovery and rendezvous into consideration, numerous active slots for direct discovery and rendezvous can be reduced.

Figure ?? gives a concrete example about such direct and indirect interactions in the neighbor discovery protocols. Three devices $S$, $A$ and $B$ have already discovered...
each other. Based on a state-of-the-art discovery protocol Disco [12], a schedule is given in Fig. ??, where $S$, $A$ and $B$ asynchronously begin their rendezvous cycles in global time slots 1, 0 and 0, respectively. Two devices being active at the same slot indicates a rendezvous. As a result, $S$ will rendezvous with its already discovered neighbor $A$ and $B$ in global slots 4 and 7, respectively, via direct communications with each of them. Moreover, $S$ will continue to directly discover new neighbors in the global time slot 1, 4, 7 and 10. However, we can see that in the global time slot 0, $A$ has already rendezvoused with $B$ by exchanging neighbor tables. Therefore, when $A$ and $S$ rendezvous in the global time slot 4, $A$’s neighbor table containing the neighbors of $B$ will propagate to $S$. As a result, even if $S$ does not activate its radio in the global slot 7 to directly rendezvous with $B$, $S$’s rendezvous with $B$ can still be achieved indirectly through two other rendezvous (i.e., the rendezvous between $B$ and $A$, and the rendezvous between $A$ and $S$). This is an example how neighborhood information propagates indirectly by bridging multiple pairwise communications, which opens the possibility to eliminate the need for fully meshed pairwise discovery and rendezvous. Since the above schedule is known to $S$ after the first time $S$ discovers $A$ and $B$, $S$ eliminates some of its active slots yet still achieving the indirectly rendezvous.

2.2 Energy Conservation

To intuitively show the effectiveness of the indirect interaction, we plot our testbed results for Disco [12] and its $EQS$ assisting version, Disco+$EQS$, which takes the indirect interaction into account, as in Fig. ?? The detailed testbed setup is given in Section 6.

Under the networks with an average duty cycle 10%, as the device density increases, the gap on an average duty cycle between Disco and Disco+$EQS$ is interestingly enlarged. When four devices are in the networks, $EQS$ reduces 7% of total active slots in the networks, i.e., 9.3% vs. 10%. When the number of devices becomes larger, e.g., 10, $EQS$ is capable of reducing 27% of total active slots, i.e., 7.3% vs. 10%. This energy gain of Disco+$EQS$ comes from the reduction of active slots based on indirect interaction, e.g., discovery and rendezvous. It indicates that with more devices in the networks, $EQS$ reduces more active slots based on the enriched indirect information propagation among devices. Therefore, Fig. ?? illustrates the design goal of $EQS$, which filters out redundant active slots to conserve energy, i.e., enlarging the dashed area between two lines.

2.3 Design Motivation

Given the existence of a plethora of discovery and rendezvous protocols, in Section 4 we decide to design $EQS$ as a transparent augmenting middleware filter on the bottom of them. Given any schedule based on these protocols, $EQS$ transparently filters out the redundant active slots according to indirect discovery and rendezvous. It provides a unified solution for highly diverse, heterogeneous discovery and rendezvous protocols that may be deployed at individual mobile devices from various mobile applications. Based on this transparent and non-intrusive design philosophy, we do not consider to synchronize devices by adding common active slots. In fact, we consider how to deactivate the slots supposed to be active, not vise versa. Note that the deactivation of certain active slots may lead to the fact that a new neighbor cannot be discovered by some devices in the networks immediately. But with rendezvous services, the devices already discovering each other function as a group, and thus a device finding a new neighbor leads to a quick propagation of neighborhood information to others.

According to the above design philosophy, we face two design challenges: How to capture above indirect nature of neighborhood information propagation, and how to leverage such a nature to adaptively filter out redundant active slots to conserve the energy. To address these two challenges, we first propose a theoretical concept called extended quorum system to capture the indirect propagation as in Section 3, and then we present our main design to filter out the redundant active slots to conserve the energy as in Section 4.

3 THEORETICAL BACKGROUND

In this section, we introduce the theoretical concepts for neighbor discovery and rendezvous maintenance. In Section 3.1, we first present a concept called quorum graph, and we then give one of its key propriety called reachability; in Section 3.2, based on the reachability of quorum graphs, we first propose two special quorum graphs called legacy quorum system and extended quorum system, and we then discuss their utilization in neighbor discovery and rendezvous schemes; in Section 3.3, based on the legacy and extended quorum systems, we define a quorum reachability minimization problem to minimize the energy usage in neighbor discovery and rendezvous, and then we discuss its complexity.

3.1 Quorum Graph

3.1.1 Definition of Quorum Graph

A quorum graph is a graph representation $G(V,E)$ (e.g., Fig. 2) of a neighbor discovery and rendezvous maintenance schedule (e.g., Fig. 1). We present the formal definition of a quorum graph as follows.

Definition 1: Quorum Graph. Given a Discovery and Rendezvous Schedule $DRS$ for devices, a corresponding quorum graph $QG$ is a supergraph consisting of several non-overlapping subgraphs of vertices, which is characterized by five following features.

1) Vertex: every active slot of a device in $DRS$ can be represented as a vertex;
2) **Subgraph**: all the vertices corresponding to all active slots for the same device can be represented as a subgraph, called a quorum;

3) **Supergraph**: all the subgraphs corresponding to all the devices can be represented as a supergraph, i.e., $QG$;

4) **Horizontal Edge**: If two vertices correspond to the same active slot in two different subgraphs, then a bidirectional horizontal edge exists between them, which indicates that in this slot two devices corresponding to two subgraphs can bidirectionally exchange neighborhood information;

5) **Vertical Edge**: If two vertices correspond to the different active slots in the same subgraph, then an unidirectional vertical edge exists between them from the early slot to the later slot, which indicates that this device corresponding to the subgraph can only unidirectionally pass neighborhood information; it has learnt in the early slot to the later slot, not vice versa. As a result, the vertical dashed edges are top-down only.

Based on the above discussion, in Fig. 2, (i) a row of vertices represents the duplicated copies of the same active slot for different devices; (ii) a column of vertices represents the different active slots for the same device; (iii) the edges between two vertices represent the links for neighborhood information propagation through networks along with time dimension.

To illustrate how to construct a quorum graph based on a schedule, in Fig. 1 and Fig. 2, we provide a walk-through of quorum graph construction. (i) Building four subgraphs (quorums) based on four devices in the schedule. (ii) According to the number of active slots in every device, building the same number of vertices in every subgraph, e.g., we build three corresponding vertices, i.e., $A2$, $A4$ and $A5$ in a subgraph $A$ for device $A$. (iii) Building unidirectional edges within subgraphs from the vertices associated to early slots to the vertices associated to later slots, e.g., we build two unidirectional edges from vertex $A2$ to $A4$ and $A5$, respectively. (iv) Building bidirectional edges for the vertices in different subgraphs but associated to the same slots, e.g., we build a bidirectional edge from vertex $A2$ to $C2$, since these two vertices are associated to the same slot, i.e., slot 2.

The rationale behind the quorum graph construction is that with this quorum graph we can capture the neighborhood information propagation among the devices along the time dimension. For bidirectional edges, in Fig. 2, device $A$ and $C$ will rendezvous with each other in a bidirectional way in slot 2, which is the reason why a bidirectional edge exist between $A2$ to $C2$. For unidirectional edges, in Fig. 2, when device $C$ and $D$ rendezvous with each other in slot 3, $C$ will pass the information about $A$ to $D$, but $C$ cannot pass the information about $D$ to $A$ in slot 2, since $C$ will rendezvous with $D$ after slot 2, i.e., slot 3. This is the reason why in Fig. 2 the edge between $C2$ to $C3$ are unidirectional. By the above example, a quorum graph represents a high level abstraction about how neighborhood information propagates among the devices based on their rendezvous along the time dimension.

### 3.1.2 Reachability

Based on the quorum graph obtained in the last subsection, we present a key property of the quorum graph, i.e., reachability. In the traditional Graph Theory [15], reachability is the notion of being able to access from one vertex in a directed graph to some other vertices. However, under the quorum graph context, we employ the reachability to describe the capability of subgraphs, instead of vertices, to reach each other in a given quorum graph.

**Property 1: Reachability.** In a quorum graph, if every quorum can reach at least one vertex in every other quorum, then this quorum graph has reachability. Further, if every quorum can reach every other quorum only by its own vertices, instead of the vertices of other quorums, then this quorum graph has direct reachability; otherwise, it has indirect reachability.

For example, Fig. 3 shows three different quorum graphs, i.e., $QG_1$, $QG_2$ and $QG_3$. (i) $QG_1$ has the direct reachability, since in $QG_1$, every quorum has at least one vertex that can directly, with one-hop, reach all other quorums by the vertices in its own quorum. (ii) $QG_2$ has the indirect reachability, since in $QG_2$, some quorums have to leverage other quorums’ vertices for reachability, e.g., vertex $A2$ in quorum $Q_A$ can reach vertex $D3$ in quorum $Q_D$ with the vertices in quorum $Q_C$, i.e., vertex $C2$ and $C3$. This is the only path that $Q_A$ can reach $Q_D$. (iii) $QG_3$ has no reachability, since in $QG_3$, no vertex in $Q_C$ can reach $Q_D$.

Considering the neighbor discovery and rendezvous context, the reachability of a quorum graph indicates how neighborhood information about one device can propagate to other devices, directly by itself or indirectly by others.

### 3.2 Quorum System

In this subsection, via the quorum graph, we introduce a theoretical model, *Legacy Quorum System*, used by
current neighbor discovery and rendezvous protocols [9] [10] [11] [16] [12] [13]. Then, we improve this legacy quorum system by an extended quorum system.

3.2.1 Legacy Quorum System

Definition 2: Legacy Quorum System. A legacy quorum system $LQ$ is a quorum graph with direct reachability among any pair of quorums.

In Definition 2, under the neighbor discovery context, this direct reachability among any pair of quorums indicates the direct discovery or rendezvous for every two devices. Thus, Definition 2 presents a model used by current protocols for pairwise and direct discovery and rendezvous. For example, in Fig. 3, among three different quorum graphs, $QG_1$ is a legacy quorum system, since $QG_1$ has direct reachability, while $QG_2$ and $QG_3$ are not. Under our context, Definition 2 can be employed to verify a given schedule whether or not can lead to a pairwise and direct discovery and rendezvous between devices.

3.2.2 Extended Quorum System

In this subsection, based on quorum graph and legacy quorum system, we define a new kind of models for neighbor discovery and rendezvous with the indirect nature. Our motivation about this new kind of model is based on the fact that in the legacy quorum system, each quorum reaches other quorums directly by its own vertices, and no intermediate quorum is involved to assist the reachability among quorums in an indirect way. In Fig. 3, the legacy quorum system only makes use of the horizontal solid edges, and our new model tries to employ the vertical dashed edges to achieve more diverse reachabilities in the same quorum graph. Similar to Definition 2, we give the definition of this new model by the quorum graph.

Definition 3: Extended Quorum System. A extended quorum system $EQ$ is a quorum graph with indirect reachability among any pair of quorums.

In Definition 3, under the neighbor discovery context, the indirect reachability indicates the indirect interaction between devices. Thus, Definition 3 presents a model for indirect discovery and rendezvous. For example, in Fig. 3, $QG_2$ is an extended quorum system, since $QG_2$ has indirect reachability; while $QG_1$ and $QG_3$ are not. Under our context, Definition 3 can be employed to verify a given schedule whether or not can lead to indirect discovery and rendezvous between devices.

3.2.3 Relationship of Direct and Indirect Discovery

Let $A$, $B$, $C$ and $D$ be four devices in the networks, whose schedules are given by a corresponding quorum graph $QG_1$ in Fig. 4. Based on Definition 2 in Section 3, we can easily verify that $QG_1$ is a legacy quorum system, since a simple traversal will show that $QG_1$ has direct reachability. Based on the assumptions, it ensures all the devices can successfully and directly discover and rendezvous with others.

However, a new schedule $QG_2$ that is obtained by reducing some active slots in $QG_1$ based on extended quorum system can still achieve discovery and rendezvous, when some devices have already discovered each others. Let $QG_2$ in Fig. 4 be a new schedule. Based on Definition 3, we can easily conclude that $QG_2$ is an extended quorum system, since a simple traversal will show that $QG_2$ has indirect reachability. In $QG_2$, the neighborhood information about device $B$ can be propagated to $A$ via $A_4$, to $C$ via $C_4$, and to $D$ via $A_5$ and $D_5$, i.e., via already discovered neighbors. There are similar situations to the information for $A$, $C$ and $D$.

From above example in Fig. 4, we can see that the key difference between $QG_1$ and $QG_2$ is that $QG_1$ does not take discovered devices into consideration, since the legacy quorum system only focuses on pairwise and directly discovery and rendezvous. However, when some neighbors have been already discovered, the schedules based on extended quorum system can make indirectly discovery and rendezvous with fewer active slots. For example, in $QG_2$, the information of $B$ can be propagated to $D$ indirectly via intermediate $A$. Whereas, if we still use $QG_1$ as rendezvous schedule where no intermediate device is considered, then it will lead to redundant active slots. How to obtain a new schedule (based on legacy quorum system) with minimal active slots (based on an extended quorum system) from a given discovery schedule is the key problem we aim to investigate. The formal definition of this problem is given in next subsection.
3.3 Quorum Reachability Minimization Problem

We present a quorum reachability minimization problem for neighbor discovery and rendezvous maintenance.

**Definition 4: Quorum Reachability Minimization Problem.** Given a quorum graph representing legacy quorum system, Quorum Reachability minimization Problem, QRP, is to select minimal number of vertices to maintain reachabilities between every two quorums, forming a new quorum graph representing extended quorum system.

Under our context, by distributedly solving QRP, all devices already discovering each others will obtain the same schedule for the networks based on extended quorum system. Moreover, by distributedly filtering out the redundant active slots not in this new schedule, the better energy performance can be achieved.

Before presenting the solution for QRP, we evaluate its complexity. We prove that QRP is NP-hard by reducing set covering problem to it. Due to the space limitation, the proof is given in [17].

4 EQS Design

In this section, we present some preliminaries network models, and then we propose our main design EQS, which is a heuristic solution to a NP-hard quorum reachability minimization problem that obtains an extended quorum system from a legacy quorum system, along with an example about EQS.

4.1 Network Model

For the networks of static devices with always-available radio, discovery and rendezvous are trivial, since simple broadcasts can enable all neighbors to discover a device [9]. However, for the networks of mobile devices with constrained radio usage, both the discovery and the rendezvous become complicated [12]. Time synchronization will be greatly helpful, but involves considerable and unaffordable cost [14]. Some related work, e.g., [9], has been proposed to employ the legacy quorum system to tackle the discovery and the rendezvous for asynchronous mobile networks with duty cycled devices.

Since our design should be compatible with current discovery and rendezvous, we present the similar network model and assumptions [12] [13] [14]. (i) In single-hop networks, time is divided into slots with equal lengths. (ii) The radios of devices in networks are activated in certain active slots according to a given schedule based on the legacy quorum system. (iii) In both beginning and end of an active slot, a device broadcasts its two-hop neighbor table. (iv) An overlapping of active slots between devices indicates a discovery or a rendezvous. Note that even with the clock drift, since a device broadcasts twice in both beginning and end of an active slot, a partial overlapping in an active slot can still guarantee a successful bidirectional discovery. (v) Every device distributedly collects and maintains neighborhood.

4.2 Main Design

In this subsection, given a schedule based on the legacy quorum system, we propose a design, EQS, which outputs a filter vector, FV, by solving quorum reachability minimization problem. By the filter vector FV, a device in the networks can filter out the unnecessary active slots for neighbor discovery and rendezvous maintenance.

The main idea of our heuristic scheme EQS is simple and based on two following observations. (i) Given a quorum graph, we have to select a new subgraph with the minimal number of vertices to maintain the reachabilities for every two quorums, and then filter out other unselected vertices. In our discovery scenario, given a schedule, we have to select the minimum number of active slots to maintain reachabilities for every two devices in the networks, and the filter out other redundant active slots to conserve energy, i.e., given total N devices, total N × (N−1) reachabilities (every N device for every other N−1 devices) have to be maintained with minimal number of active slots. (ii) Every time we shall select some active slots that should provide the maximal contribution to total N × (N−1) reachabilities for all the quorums, and the minimum overhead to the reachabilities between themselves.

For the minimum overhead to reachabilities, selecting a row of vertices together at a time will obtain the minimum overhead for reachabilities between themselves, since the vertices in the same row will always reach each others, i.e., no extra effort should be made for the reachabilities of the vertices belonging to the same row.

For the maximum contribution to reachabilities, the contribution of a row x, Cx, is computed as follows. Cx = T x N x, where T x is the number of new provided reachabilities after selecting the vertices in row x; N x is the number of the vertices in row x. By the above formula, every time we select few efficient vertices to provide the maximum contributions to total reachabilities (maximum T x) with the minimal number of active slots (minimum N x).

Therefore, our scheme is that every time we select a row of vertices such that this row will contribute to minimum remaining portion of total N × (N−1) reachabilities, until already selected vertices can maintain all total N × (N−1) reachabilities. This is the key idea of our scheme. However, since we select a row of vertices as a whole, some vertices in this row may not contribute to the total N × (N−1) reachabilities. Therefore, after every selection of a row of vertices, we delete the vertices that do not contribute to the total N × (N−1) reachabilities.

After obtaining the complete subgraph, EQS outputs a 0-1 filter vector FV where 1 indicates corresponding active slot remains and 0 indicates otherwise. By this FV and the original neighbor discovery schedule, every device in the networks can maintain the discovery and rendezvous with fewer active slots. This FV is constantly changed by EQS with an online updating process according to the latest neighborhood information in a device’s lifecycle.

Fig. 5 gives an example about EQS.
Fig. 5. Example of \textit{EQS}

1) Based on a given schedule, we can obtain its corresponding quorum graph. The reachabilities after every step is shown in the above left corner table, where 0 indicates that the reachability from row to column is not maintained, and 1 indicates otherwise.

2) Based on its quorum graph, we compute the contribution per vertex of every row to the total $4 \times (4 - 1)$ (i.e., $N \times (N - 1)$) reachabilities. For example, the contribution of the first row $C_1$ is $\frac{2 + 1}{4} = 1$, since selecting vertex $B_1$ and $D_1$ to the subgraph only contributes two reachabilities, i.e., from $Q_B$ to $Q_D$ as well as from $Q_D$ to $Q_B$. By the same method, we compute that $C_4$ is the local maximal in the first round and is $\frac{4}{3} = 2$. Therefore, we select the 4th row of vertices to the subgraph by marking them to grey as in Step 2.

3) In the remaining quorum graph, $C_1$ and $C_3$ have the same maximal value, which is $\frac{4}{3} = 2$. We select 1st row according to the alphabetical order.

4) After we select the 1st row to subgraph, only two reachabilities need to be maintained shown by the table. The 5th row has the local maximal contribution with $C_5 = \frac{2}{2} = 1$, so we select 5th row. After this, all reachabilities are maintained, and we complete the subgraph by reducing other unselected vertices. By changing the subgraph to its adjacent matrix, every device can distributedly choose its own column to obtain its $FV$. For example, device $A$ chooses \{0, 0, 0, 1, 1\} as its $FV$. Therefore, when upper-layer discovery and rendezvous protocol activates $A$ in 2nd slot, $FV$ of $A$ will filter out this active slot and makes $A$ maintain inactive.

Via the above example, we can see that \textit{EQS} takes the legacy quorum system based schedules as input, and outputs a $FV$ for every device, by converting this schedule to a new schedule based on the extended quorum system. After obtaining this $FV$ consisting of $0$s and $1$s, in every slots, a device will conduct logic intersection between $FV$ and Schedule Vector $SV$, which is a schedule for device itself (If discovery and rendezvous protocol requires this slot to be active, then the corresponding bit on $SV$ is 1, and \textit{vice versa}). Therefore, only both corresponding bits on $FV$ and $SV$ are $1$, then a device will activate itself in this slot. If the corresponding bit on $FV$ is $0$ and the corresponding bit on $FV$ is $1$, then $FV$ filters this active slot out, since based on extended quorum system this slot is no longer necessary to be active.

5 \textbf{Simulation Evaluation}

To evaluate the effectiveness and flexibility of our \textit{EQS} design, in this section we integrate \textit{EQS} with two state-of-the-art discovery and rendezvous protocols:

- Disco \cite{et} by Dutta \textit{et al.} in SenSys’08.
- U-Connect \cite{kandhalu} by Kandhalu \textit{et al.} in IPSN’10.

To understand how much energy efficiency \textit{EQS} can offer, we also compare \textit{EQS} with a Baseline design, which filters out the same amount of active slots with \textit{EQS}, but \textit{at random}, instead of employing extended quorum system. Thus, we simulate three versions of above protocols, \textit{i.e.}, original, Baseline and \textit{EQS}.

5.1 Simulation Setup

In our simulation, 100 mobile devices are uniformly deployed in a square area of size $200m \times 200m$. The transmission ranges of devices are set from $20m$ to $110m$, which leads to average mobile device densities from 3.6 to 55.36 neighbor devices. For the mobility model of mobile devices, we use the random waypoint model \cite{8} \cite{9} \cite{10}, with the average device velocity setting to be $1m/s$. Each simulation is repeated 20 times and the average results are reported.

Three groups of simulations are conducted. (i) To show the performance gain, the key metric energy consumption, represented by Average Duty Cycle (ADC) of devices in the networks, are evaluated with different Device Densities (DD). (ii) The impact of different Duty Cycles (DC) on energy consumption is also shown. (iii) The reduction of active slots for the energy consumption in \textit{EQS} may increase the Discovery Latency (DL). To verify the impact of the reduction of active slots on DL, we also show the CDF of discovery and rendezvous.

5.2 Impact of Device Density

The impact of device densities on energy consumption, represented by Average Duty Cycle (ADC) of all the
In this subsection, we investigate the impact of device’s duty cycle on the energy consumption, which is also shown by the average duty cycles of all schemes increase. Since no reduction of active slots is preformed in Disco and U-Connect, in both figures the increase of average duty cycles of Disco and U-Connect is steady. Because reductions in number of active slots in Baseline and EQS are the same, the curves of them overlap with each other all the time. In Figure 8, we can see that when the duty cycle is 8%, the average duty cycle of devices under Disco+EQS obviously outperforms that under Disco with a performance gain of 13.7%. As the duty cycle increases to 20%, this performance gain is also enlarged to as much as 40%. In Figure 9, even though not as much as it outperforming Disco, EQS still has a maximal 31% energy performance gain over U-Connect.

5.4 Impact of Reduction of Active Slot

We plot the CDF of the number of discovery for both of schemes in Figure 10 and Figure 11. In these figures, as more discovery time is allowed (i.e., increasing cumulative discovery latency), the percentages of discoveries also increase for all schemes. However as in Figure 10, the devices under Disco and Disco+EQS are able to discover neighbors much faster than under Disco+Baseline. This is because Disco+Baseline only reduces active slots at random, which leads to a maximal 40% lower performance. As for Disco and Disco+EQS, even though Disco+EQS reduces some of active slots to conserve energy, the reduction of EQS is based on extended quorum system, not at random. Therefore, under Disco+EQS, neighborhood information propagation assists devices to find their new neighbors based on already discovered ones. In fact, this neighborhood information propagation enables some devices to discover each other earlier under Disco+EQS than under Disco itself, which in part compensates for reductions of active slots. For example, in Figure 10, in the end of discovery process, EQS enables devices to make a 4% faster discovery than the devices under Disco. This is because with the increase of discovery latency, the cumulative effect of neighborhood information propagation becomes more obvious, which leads to an more effective discovery. The similar phenomenon is observed in Figure 11.

6 Testbed Evaluation

In Section 5, we have shown that EQS effectively reduces energy consumption for discovery and ren-
6.2 Impact of Duty Cycle
Figure 14 shows the impact of different duty cycles on the energy consumption, shown by average duty cycle. In the testbed experiment, when the duty cycle is low, e.g., 4%, no reduction is performed by EQS since a low device density and a low duty cycle lead to fewer total active slots which cannot form an extended quorum system. However, when the duty cycle becomes bigger, e.g., 10%, EQS can reduce 17% active slots according to the extended quorum system. When the duty cycle becomes 20%, EQS achieves the maximal energy performance gain, i.e., 21.5%. This maximal energy performance gain is smaller than what we obtained in large-scale simulation. This is because in the simulation EQS is under much larger and denser networks than in the testbed. This may indicate that EQS is more suitable for large-scale networks.

6.3 Impact of Reduction of Active Slot
Figure 15 plots the testbed experiment results on the CDF of discovery. From this figure, we can see that Disco+EQS continues to exhibit a similar performance, compared with Disco itself. However, in the testbed experiment, Disco+EQS outperforms Disco in the later half of discovery process by 6%. The similar results are observed in Figure 10, but the performance gain is smaller. Again, as observed in Figure 10, Disco+Baseline has a much worse performance compared with others, and the devices under Disco+Baseline only discover 51% of their neighbors, when the devices under Disco+EQS and Disco have discovered all their neighbors.

7 Trace-Driven Evaluation
In this section, we evaluate EQS with a real-world taxi GPS trace dataset. We first present our evaluation methodology, and then we show impacts of device density, duty cycles, and discover latency on the performance of EQS, respectively.

7.1 Methodology

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Fig. 17. Statistics
In this trace-driven evaluation, our dataset consists of 6 months of GPS traces from 14,453 taxis in the...
Chinese City Shenzhen. The data are collected by the Shenzhen government for the urban transportation pattern research. Each taxi uploads records on an average of every 30 seconds, with each record consisting of the following parameters: (i) Plate Number; (ii) Date and Time; (iii) GPS Coordinates; and (iv) Availability: with a passenger or not when the record is uploaded to the dispatch center. Figure 17 summarizes details of the used datasets. Based on the above GPS trace records, we have a real-time location trace of every taxi in the networks.

Figure 16 shows a taxi drop distribution in Shenzhen downtown area based on a one-hour uploading window in the rush hour of one day, i.e., 5PM. Yellow points indicate individual taxi GPS locations, and the lighter the area, the denser the taxi density.

Figure 16. Distribution of Taxis

Based on this dataset, we perform a trace-driven evaluation to verify how EQS can reduce the communication overhead in this taxi network if taxi drivers want to find nearby taxis by neighbor discovery. Note that different from regular sensor networks, a taxi network does not have energy constraints, but reducing active slots for neighbor discovery can also minimize the communication overhead for bandwidth efficiency. Essentially, we treat this taxicab network as a mobile network where every taxicab is a mobile device with unique a mobility pattern. We test the impact of cumulative discovery latency on the percentage of discoveries. Further, we test the impact of different device density (by changing communication ranges of taxis) and different duty cycles on energy consumption. With a default duty cycle 10% (equal to the uploading speed of GPS record) and 500m communication range, we compare EQS with Baseline and Disco as in the testbed experiment.

7.2 Impact of Device Density

In this subsection, we report the effectiveness of EQS for energy conservation in our trace-driven evaluation. Figure 18 shows the impact of the device density in terms of communication range on average duty cycles. As the increase of the device density, the average duty cycle of Disco keeps the same and those of Disco+Baseline and Disco+EQS decrease, because they filter out the same number of active slots. But we found that when low densities, e.g., 10, there is no reduction of average duty cycle under Disco+EQS. When the density increases, the performance gain also increases, shown by reduced average duty cycle. This is because low densities cannot form an extended quorum system for the reduction of active slots in the taxi network, but when density increases, an extended quorum system can be formed to reduce the redundant active slots.

7.3 Impact of Duty Cycle

Figure 19 shows the impact of different duty cycles on the average duty cycle in our trace-driven evaluation.

We found that when the duty cycle is low, e.g., from 0% to 8%, reduction is limited by EQS since a low duty cycle leads to fewer total active slots which cannot form an extended quorum system. But as the duty cycle becomes higher, e.g., 14%, EQS significantly reduces average duty cycle compared to Disco. This maximum energy performance gain is large than we obtained in large-scale simulation. This is because in our trace-driven simulation, the density of taxicabs is much higher than that of simulation. This indicates that EQS works better in denser networks.
7.4 Impact of Device Discovery Latency

Figure 20 plots the trace-driven evaluation results on the CDF of discovery. From this figure, we can see that Disco+EQS continues to exhibit a similar performance to Disco but significantly better than Disco+Baseline only discover 73% of their neighbors, when the devices under Disco+EQS and Disco have discovered all their neighbors.

8 EQS-Dispatch Application

In this section, to prove the real-world value of EQS, we propose and evaluate an application called EQS-Dispatch with which in a taxicab network, taxi drivers quickly navigate optimal directions to cruise the road segments to optimize pickup by an EQS assisted neighbor discovery.

8.1 Application Background

Specifically, in our application, at an intersection, an empty-taxicab driver would select a direction with fewer empty taxicabs to avoid competition, thus increasing the change of picking up a new passenger. A trivial solution to this problem is to install a centralized system, which can be used to collect the information from nearby taxis in terms of locations and status. But such a system requires that each taxi has with cellular data connectivity, which leads to a potential cost. We are thus faced with the challenge of obtaining taxi status with no extra hardware installation on the taxis. In this work, we envision that individual taxi drivers are equipped a smart phone with a peer-to-peer communication interface, e.g., ad hoc WiMax or ad hoc WiFi, and can install an app to obtain the status of nearby taxis. Taxi drivers with this app can optimize their profits by acting as a group of common interest. The drivers with this app can cruise to the areas with a low density of empty taxis, thus to maximize pickups (and thus profits). Our proposed neighbor protocol plus EQS enables a drive use few active slots to learn status of nearby taxis, which leads to reduced communication overhead, thus more bandwidth for other applications.

In our application, every taxicab broadcasts its own status record (i.e., date and time, availability, direction, GPS coordinates, etc) to its neighboring taxis with in the communication range. The broadcast is based on Disco and Disco+EQS. According to the information collected, when a taxi driver navigates to the optimal directions, as determined by the number of nearby empty taxis. This metric can potential maximize the probability of picking up the next nearby passengers due to the absence of competing taxis. Based on the distributions of nearby empty taxis, EQS-Dispatch can maximize the possibility of picking up passengers by guiding a taxi to a direction with fewer empty taxis.

8.1.1 Application Evaluation

In this section, we evaluate the performance of EQS in navigation for taxis in EQS-dispatch. With a total duty cycle 1/10, we compare 3 navigating results based on different discovery results of discovery schemes.

(i) Dispatching with Disco; navigating taxis with results of Disco;
(ii) Dispatching with Disco+EQS; navigating taxis with results of Disco+EQS;
(iii) Dispatching with Disco+Baseline: navigating taxis with results of Disco+Baseline as in the previous evaluation.

Under all dispatching, a taxi has the same preferable directions for fewer competing empty taxis. But since the employed discovery schemes are different, a dispatching with a faster discovery scheme may achieve better performance. The performance is characterized by two metrics: empty taxis density and an average duty cycle (for communication overhead). To show the difference with or without our EQS-dispatch, we also compare the above 3 schemes with Ground Truth without Navigation, where the density is computed based on original taxi traces without altering the routes of any taxis. Note that given the density of competing taxis, how to select the optimal route to achieve the optimal density is outside the scope of this paper. We simply let taxi drivers greedily select 1 out of 4 directions in an
intersection according to empty taxi densities in every direction and then compute densities of competing taxis in its neighborhood every minute.

We investigate the densities of empty taxis in three different dispatching strategies. We report the results of navigating taxis using a 3KM communication radius in Figure 21. We found that with the increase of the cumulative driving time, all dispatching schedules have decreasing density of empty taxis, but the dispatching based on Disco and Disco+EQS has better performance than the dispatching based on Disco+Baseline. This is because Disco and Disco+EQS can discover neighboring taxis faster, which makes it go to the direction with low density of empty taxis faster. Compared to Disco, even though dispatching based on Disco+EQS has slighter lower performance but dispatching based on Disco+EQS is more efficient, since it has less communication overhead as shown before.

9 RELATED WORK

Neighbor discovery and rendezvous maintenance in low-power mobile networks has been extensively studied in the literature. In general, the existing discovery and rendezvous schemes can be divided into two categories, explicitly and implicitly quorum system based. We also provide some related work about our taxi-dispatching application.

9.1 Explicitly Quorum System based Schemes

To address discovery and rendezvous problem with a bounded worst-case latency, the explicitly quorum systems based protocols ensure the existence of overlapped active slots between any pair of devices within a bounded time. In these protocols, time is normally divided into \( m \times m \) continuous slots as a matrix and each device selects one row and one column to activate its radio. Consequently, regardless which row and column a device chooses, it is guaranteed to have at least two common active time slots with other devices. The main drawback for this kind of protocols is a global parameter, which forces all devices to have the same duty cycle [9].

To support asymmetric duty-cycle setting, Zheng et al. [10] apply optimal block designs using difference sets for discovery and rendezvous in bounded latency. Based on their methods, discovery and rendezvous problem in asymmetric duty-cycle setting reduces to an NP-complete minimum vertex cover problem requiring a centralized solution [10]. More recently, Lai et al. present CQS-pair [11] and GQS-pair [16], which support heterogeneous quorum-based systems where devices can have different cycle lengths and hence different duty-cycle settings. However, only two kinds of duty cycles are supported.

9.2 Implicitly Quorum System based Schemes

Implicitly quorum system based protocols are also referred as deterministic protocols, which are proposed recently to handle the asynchronous neighbor discovery problem in mobile wireless networks [12] [13] [14]. These protocols select one or multiple prime numbers for every device to represent their duty cycles. Based on the Chinese Remainder Theorem [22] [23], these devices would have bounded discovery and rendezvous latency based their chosen duty cycles. These protocols implicitly employ the idea of quorum systems to enable every two of devices in the networks have at least one common active slots for each other. In Disco [12], each device selects a pair of prime numbers and generates its period independently based on the requirement of duty cycles.

To improve the performance of Disco, U-Connect [13] is proposed as a unified discovery and rendezvous protocol for symmetric and asymmetric duty cycle settings. U-Connect achieves higher performance compared to Disco and Quorum-based protocol, especially in asynchronous symmetric case. More recently, to improve U-Connect, WiFlock [14] combines discovery and maintenance using a collaborative beaconing mechanism with a temporal time synchronization. However, these deterministic protocols do not consider the neighborhood information propagation among the devices in the networks, which leads to redundant active slots in the networks. Our Eqs can serve as a augmenting middleware for all above discovery and rendezvous protocols to conserve more energy.

9.3 Taxi Applications

Recently data-driven applications in taxi system receive significant attention due to availability of large-scale GPS traces. Some systems are proposed to assist taxicab operators for better taxicab services, e.g., inferring mobility patterns for taxicab passengers [24], detecting anomalous taxicab trips to discover driver fraud [25], exploring carpooling opportunities [26], dispatching taxicabs based on inferred passenger demand [27] [28] [29], and discovering temporal and spatial causal interactions to provide
timely and efficient services in certain areas with disequilibrium [30]. In addition to taxicab operators, several systems are proposed for the benefit of passengers or drivers, e.g., allowing taxicab passengers to query the expected duration and fare of a planned trip based on previous trips [31], computing faster routes by taking into account driving patterns of taxicabs obtained from historical GPS trajectories [32], estimating city traffic volumes for drivers [33], and recommending a taxicab driver with a sequence of pick-up points to maximize profits [27]. But almost all these applications are based on centralized dispatching, but our application is based on distributed dispatching where a taxi learns status of nearby taxis by peer to peer communications.

10 Conclusion

In this paper, we introduce EQS, an augmenting layer to conserve energy for existing neighbor discovery and rendezvous maintenance schemes that use pairwise direct communication. Our work is mainly motivated by the insight that when devices share common neighbors, they can leverage the knowledge of each other to detect such neighbors indirectly. Thus fewer active slots are needed and energy is conserved, especially when a device needs to maintain rendezvous with previously discovered neighbors. To capture such information sharing among devices theoretically, we propose a novel extended quorum system concept where information flow paths are equivalent to graph reachability. We then propose a graph reduction algorithm EQS that filters out redundant paths but still maintains graph reachability. We have integrated our EQS design with two discovery and rendezvous protocols, and evaluated its performance with both simulations and testbed experiments. The evaluation results show that EQS can effectively filter out redundant active slots to conserve as much as 55% energy with a maximal 5% increase on latency. Finally, we propose an taxi-dispatching application called EQS-Dispatch based on EQS, and the evaluation results show that it can quickly navigate an empty taxi to a direction with few competing taxis to maximize potential profit.

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References


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