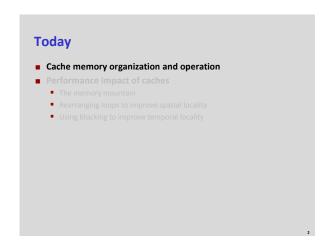
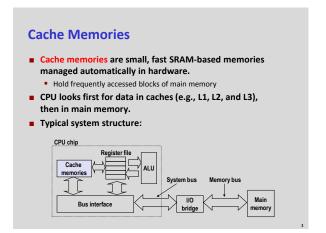
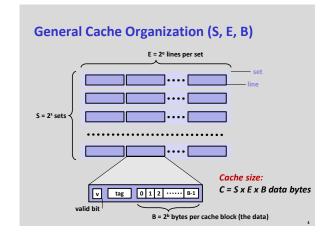
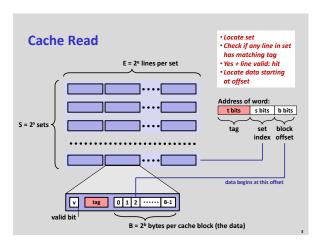
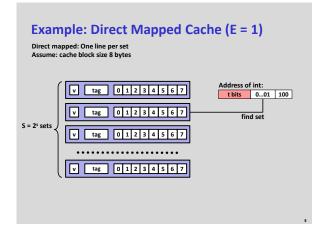
# Cache Memories CSci 2021: Machine Architecture and Organization Lecture #25-27, March 27-April 1st, 2015 Your instructor: Stephen McCamant Based on slides originally by: Randy Bryant, Dave O'Hallaron, Antonia Zhai

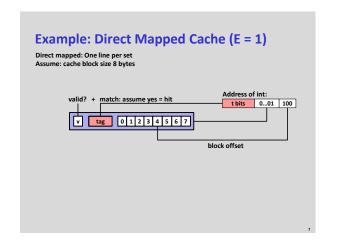


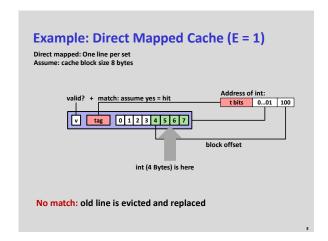


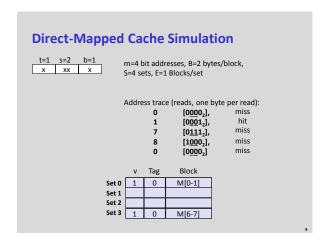


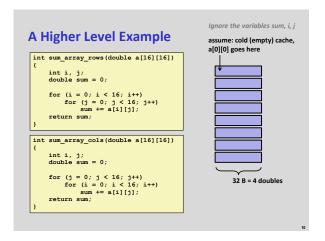


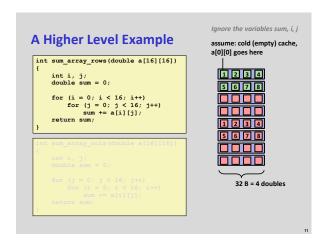


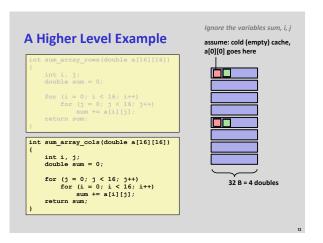


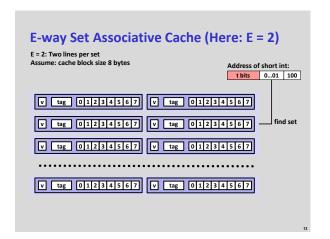


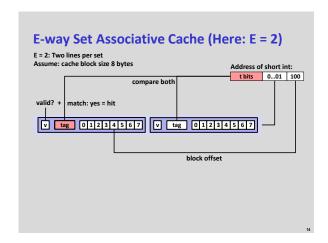


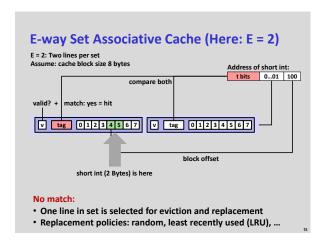


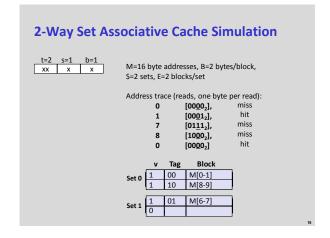


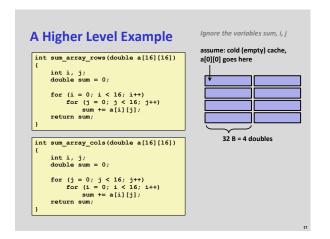


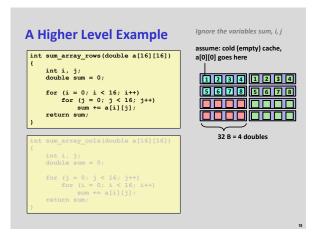


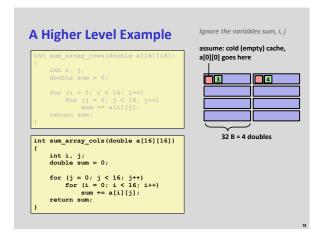






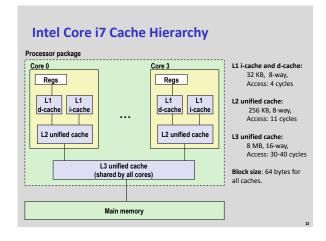








### Administrative Break We've posted several updates about the architecture lab Download new materials from the Moodle Check the forum for some clarifications



### **Cache Performance Metrics** Miss Rate Fraction of memory references not found in cache (misses / accesses) = 1 - hit rate Typical numbers (in percentages): • 3-10% for L1 • can be quite small (e.g., < 1%) for L2, depending on size, etc. ■ Hit Time Time to deliver a line in the cache to the processor. • includes time to determine whether the line is in the cache Typical numbers: 1-2 clock cycle for L1 5-20 clock cycles for L2 ■ Miss Penalty Additional time required because of a miss • typically 50-200 cycles for main memory (Trend: increasing!)

### Let's think about those numbers Huge difference between a hit and a miss Could be 100x, if just L1 and main memory Compare 99% hits vs. 97% hits? Consider: cache hit time of 1 cycle miss penalty of 100 cycles What's the ratio of average access times? Average access time: 97% hits: 1 cycle + 0.03 \* 100 cycles = 4 cycles 99% hits: 1 cycle + 0.01 \* 100 cycles = 2 cycles 99% hit rate is twice as fast! Moral: this is why "miss rate" is used instead of "hit rate"

### **Writing Cache Friendly Code**

- Make the common case go fast
  - Focus on the inner loops of the core functions
- Minimize the misses in the inner loops
  - Repeated references to variables are good (temporal locality)
  - Stride-1 reference patterns are good (spatial locality)

Key idea: Our qualitative notion of locality is quantified through our understanding of cache memories.

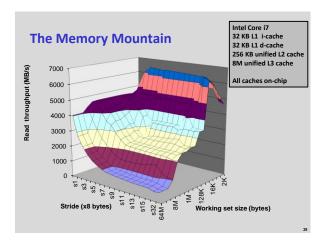
### **Today**

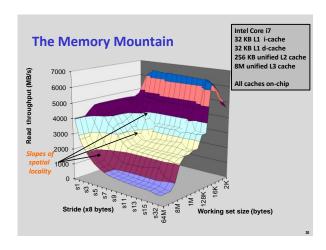
- Cache organization and operation
- Performance impact of caches
  - The memory mountain
  - Rearranging loops to improve spatial locality
  - Using blocking to improve temporal locality

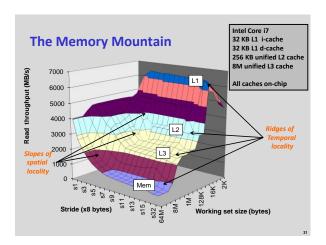
### **The Memory Mountain**

- Read throughput (read bandwidth)
  - Number of bytes read from memory per second (MB/s)
- Memory mountain: Measured read throughput as a function of spatial and temporal locality.
  - Compact way to characterize memory system performance.

### **Memory Mountain Test Function**







### **Administrative Break**

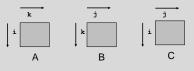
- We've heard requests for postponing the lab 4 due date
  - We're thinking about it
  - Watch for a decision announced tomorrow
- Assignment 4, on caches, out tonight
- Cache lab out next week

### **Today**

- Cache organization and operation
- Performance impact of caches
  - The memory mountain
  - Rearranging loops to improve spatial locality
  - Using blocking to improve temporal locality

### **Miss Rate Analysis for Matrix Multiply**

- Assume:
  - Line size = 32B (big enough for four 64-bit words)
  - Matrix dimension (N) is very large
    - Approximate 1/N as 0.0
  - Cache is not even big enough to hold multiple rows
- Analysis Method:
  - Look at access pattern of inner loop



### **Matrix Multiplication Example**

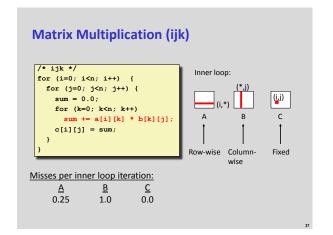
- Description:
  - Multiply N x N matrices
  - O(N³) total operations
  - N reads per source element
  - N values summed per destination
    - but may be able to hold in register

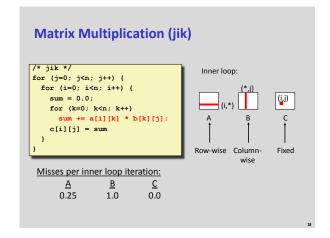
```
/* ijk */
for (i=0; i<n; i++) t

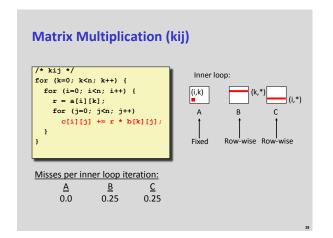
for (j=0; j<n; j++) {
    sum = 0.0;
    for (k=0; k<n; k++)
        sum += a[i][k] * b[k][j];
    c[i][j] = sum;
    }
}
```

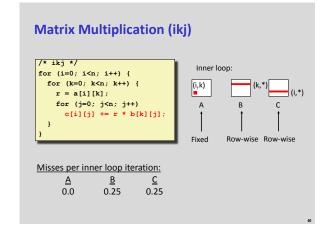
### **Layout of C Arrays in Memory (review)**

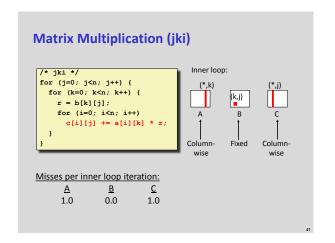
- C arrays allocated in row-major order
  - each row in contiguous memory locations
- Stepping through columns in one row:
  - for (i = 0; i < N; i++)
    sum += a[0][i];</pre>
  - accesses successive elements
  - if block size (B) > 4 bytes, exploit spatial locality
- compulsory miss rate = 4 bytes / B
   Stepping through rows in one column:
  - for (i = 0; i < n; i++)
    sum += a[i][0];</pre>
  - accesses distant elements
  - no spatial locality!
    - compulsory miss rate = 1 (i.e. 100%)

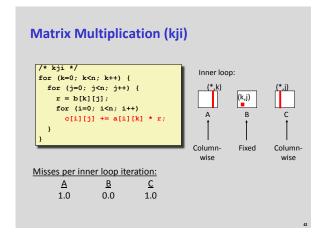




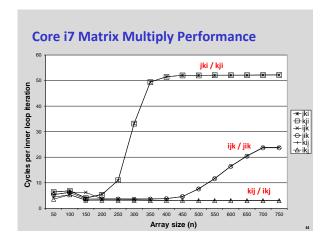




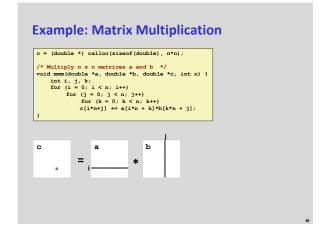


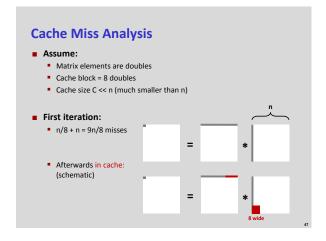


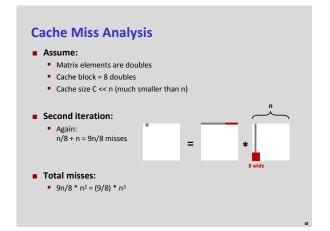
# Summary of Matrix Multiplication for (i=0; i≤n; i++) { for (j=0; j≤n; j++) { sum = 0,0; for (k=0; k<n; k++) { sum +a [i][k] \* b[k][j]; c[i][j] = sum; } } for (i=0; i≤n; i++) { for (i=0; i≤n; i++) { for (i=0; j≤n; j++) { c[i][j] += x \* b[k][j]; } } for (j=0; j≤n; j++) { c[i][j] += x \* b[k][j]; } } for (k=0; k<n; k++) { r = a[i][k]; for (i=0; i≤n; i++) { c[i][j] += x \* b[k][j]; } } for (j=0; j≤n; j++) { for (k=0; k<n; k++) { r = b[k][j]; } } for (j=0; j≤n; j++) { c[i][j] += x \* b[k][j]; } } for (i=0; i≤n; i++) { c[i][j] += a[i][k] \* x; } jki (& kji): \* place | i k kji| \* olads, 1 store \* misses/iter = 0.5 misses/iter = 0.5

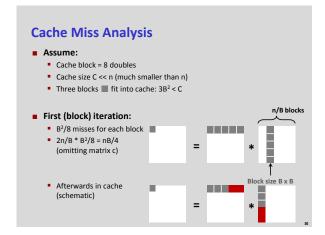


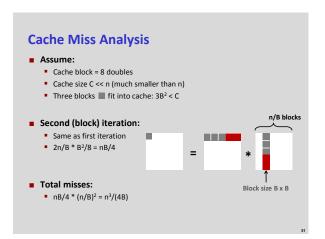
## Today Cache organization and operation Performance impact of caches The memory mountain Rearranging loops to improve spatial locality Using blocking to improve temporal locality











## Summary No blocking: (9/8) \* n³ Blocking: 1/(4B) \* n³ Suggest largest possible block size B, but limit 3B² < C! Reason for dramatic difference: Matrix multiplication has inherent temporal locality: Input data: 3n², computation 2n³ Every array elements used O(n) times! But program has to be written properly

## Concluding Observations Programmer can optimize for cache performance How data structures are organized How data are accessed Nested loop structure Blocking is a general technique All systems favor "cache friendly code" Getting absolute optimum performance is very platform specific Cache sizes, line sizes, associativities, etc. Can get most of the advantage with generic code Keep working set reasonably small (temporal locality) Use small strides (spatial locality)