Introduction to Logic Design

CSci 2021: Machine Architecture and Organization
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Overview of Logic Design

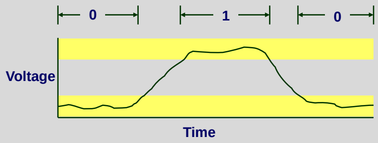
Fundamental Hardware Requirements

- Communication
  - How to get values from one place to another
- Computation
- Storage

Bits are Our Friends

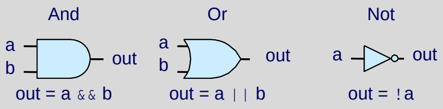
- Everything expressed in terms of values 0 and 1
- Communication
  - Low or high voltage on wire
- Computation
  - Compute Boolean functions
- Storage
  - Store bits of information

Digital Signals

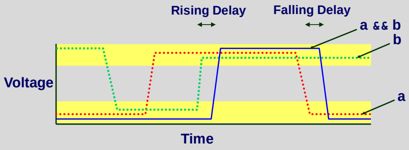


- Use voltage thresholds to extract discrete values from continuous signal
- Simplest version: 1-bit signal
  - Either high range (1) or low range (0)
  - With guard range between them
- Not strongly affected by noise or low quality circuit elements
  - Can make circuits simple, small, and fast

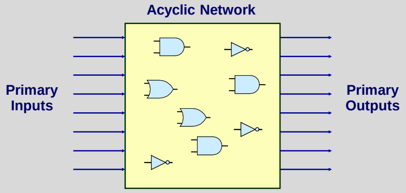
Computing with Logic Gates



- Outputs are Boolean functions of inputs
- Respond continuously to changes in inputs
  - With some, small delay



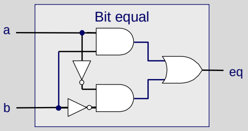
Combinational Circuits



Acyclic Network of Logic Gates

- Continously responds to changes on primary inputs
- Primary outputs become (after some delay) Boolean functions of primary inputs

Bit Equality



HCL Expression

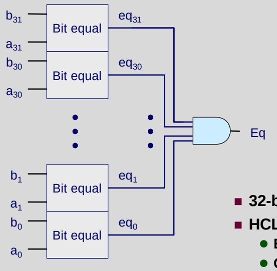
```
bool eq = (a&&b)||(!a&&!b)
```

- Generate 1 if a and b are equal

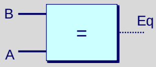
Hardware Control Language (HCL)

- Very simple hardware description language
  - Boolean operations have syntax similar to C logical operations
- We'll use it to describe control logic for processors

Word Equality



Word-Level Representation

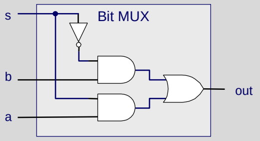


HCL Representation

```
bool Eq = (A == B)
```

- 32-bit word size
- HCL representation
  - Equality operation
  - Generates Boolean value

Bit-Level Multiplexor



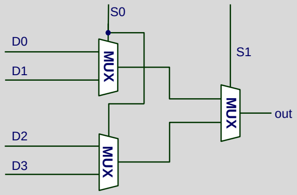
HCL Expression

```
bool out = (s&&a)||(!s&&b)
```

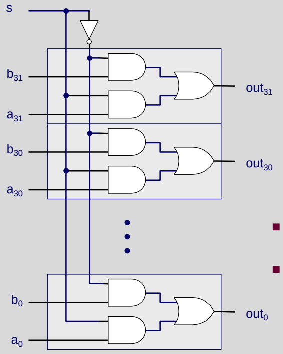
- Control signal s
- Data signals a and b
- Output a when s=1, b when s=0

Exercise Break: 4-input Mux

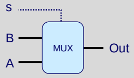
- Suppose we want to choose between 4 signals, D0, D1, D2, and D3, using two selector bits S0 and S1
- Can you build this out of 2-input muxes?



Word Multiplexor



Word-Level Representation



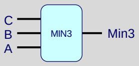
HCL Representation

```
int Out = [
  s : A;
  1 : B;
];
```

- Select input word A or B depending on control signal s
- HCL representation
  - Case expression
  - Series of test : value pairs
  - Output value for first successful test

HCL Word-Level Examples

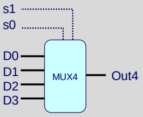
Minimum of 3 Words



```
int Min3 = [
  A < B && A < C : A;
  B < A && B < C : B;
  1              : C;
];
```

- Find minimum of three input words
- HCL case expression
- Final case guarantees match

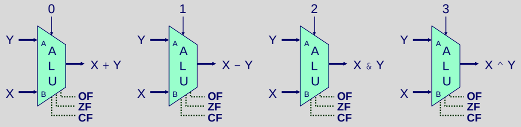
4-Way Multiplexor



```
int Out4 = [
  !s1&&!s0: D0;
  !s1     : D1;
  !s0     : D2;
  1       : D3;
];
```

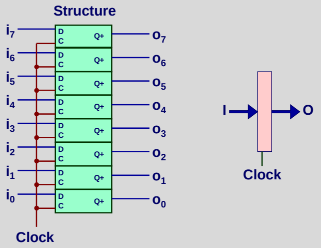
- Select one of 4 inputs based on two control bits
- HCL case expression
- Simplify tests by assuming sequential matching

Arithmetic Logic Unit



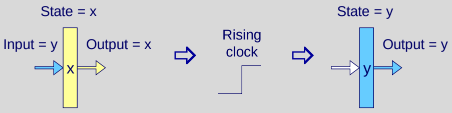
- Combinational logic
  - Continuously responding to inputs
- Control signal selects function computed
  - Corresponding to 4 arithmetic/logical operations in Y86
- Also computes values for condition codes

Registers



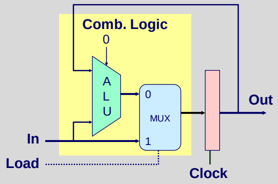
- Stores word of data
  - Different from *program registers* seen in assembly code
- Collection of edge-triggered latches
- Loads input on rising edge of clock

Register Operation

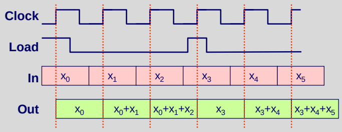


- Stores data bits
- For most of time acts as barrier between input and output
- As clock rises, loads input

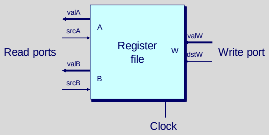
State Machine Example



- Accumulator circuit
- Load or accumulate on each cycle

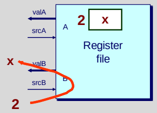


Random-Access Memory



- Stores multiple words of memory
  - Address input specifies which word to read or write
- Register file
  - Holds values of program registers
  - `%eax`, `%esp`, etc.
  - Register identifier serves as address
    - » ID 15 (0xF) implies no read or write performed
- Multiple Ports
  - Can read and/or write multiple words in one cycle
    - » Each has separate address and data input/output

Register File Timing

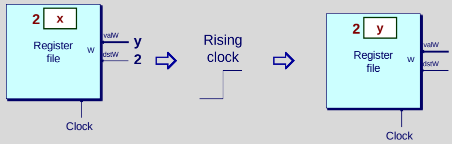


Reading

- Like combinational logic
- Output data generated based on input address
  - After some delay

Writing

- Like register
- Update only as clock rises



Hardware Control Language

- Very simple hardware description language
- Can only express limited aspects of hardware operation
  - Parts we want to explore and modify

Data Types

- `bool`: Boolean
  - `a`, `b`, `c`, …
- `int`: words
  - `A`, `B`, `C`, …
  - Does not specify word size---bytes, 32-bit words, …

Statements

- `bool a = `*`bool-expr`*` ;`
- `int A = `*`int-expr`*` ;`

HCL Operations

- Classify by type of value returned

Boolean Expressions

- Logic Operations
  - `a && b, a || b, !a`
- Word Comparisons
  - `A == B, A != B, A < B, A <= B, A >= B, A > B`
- Set Membership
  - `A in { B, C, D }`
    - » Same as `A == B || A == C || A == D`

Word Expressions

- Case expressions
  - `[ a : A; b : B; c : C ]`
  - Evaluate test expressions `a`, `b`, `c`, … in sequence
  - Return word expression `A`, `B`, `C`, … for first successful test

Summary

Computation

- Performed by combinational logic
- Computes Boolean functions
- Continuously reacts to input changes

Storage

- Registers
  - Hold single words
  - Loaded as clock rises
- Random-access memories
  - Hold multiple words
  - Possible multiple read or write ports
  - Read word when address input changes
  - Write word as clock rises